Proof Poster Activity

You will make a poster of a proof on 11x14 paper. On the poster, you should include...

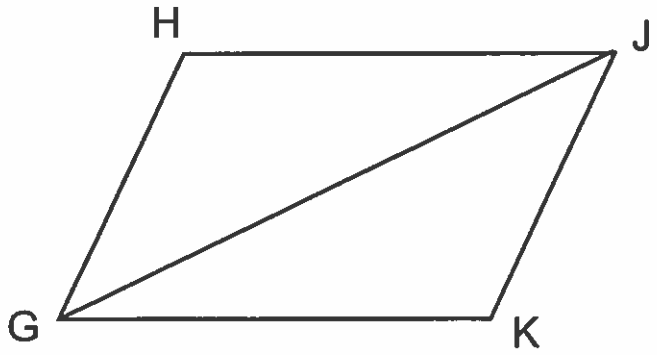
- the diagram
- the given information
- what you are trying to prove
- a 2-column proof with statements and reasons that show why the triangles are congruent

Feel free to be creative and add color! However, the most important thing is that your proof is complete and correct!

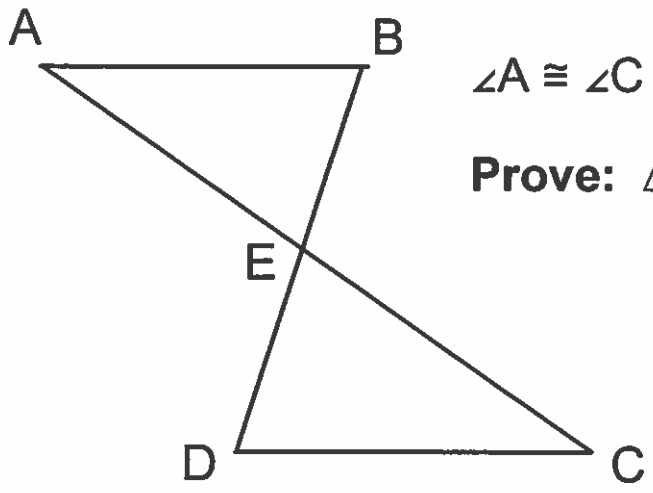
#1

Given: $\overline{HJ} \parallel \overline{GK}$; $\overline{HJ} \cong \overline{GK}$

Prove: $\Delta GHJ \cong \Delta JKG$



#2



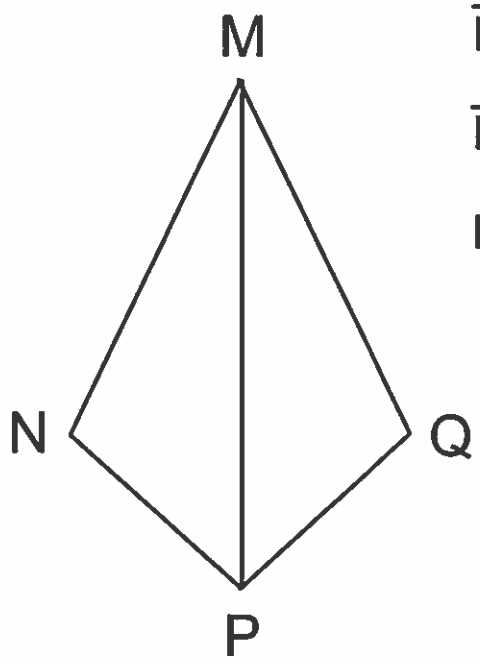
Given:

E is the midpoint of $\overline{BD}$;

$\angle A \cong \angle C$

Prove: $\Delta ABE \cong \Delta CDE$

#3



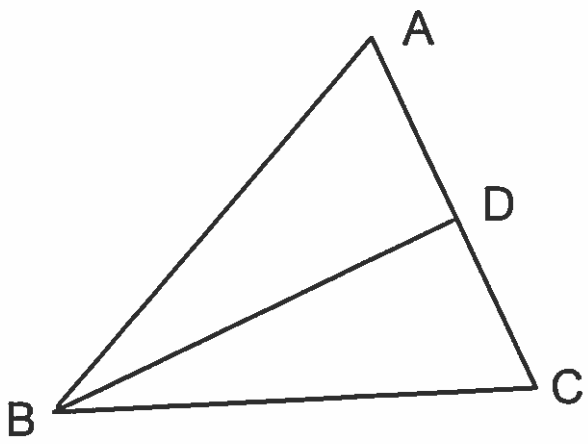
Given:

$\overline{PM}$ bisects $\angle NPQ$;

$\overline{NP} \cong \overline{QP}$

Prove: $\Delta MPN \cong \Delta MPQ$

#4

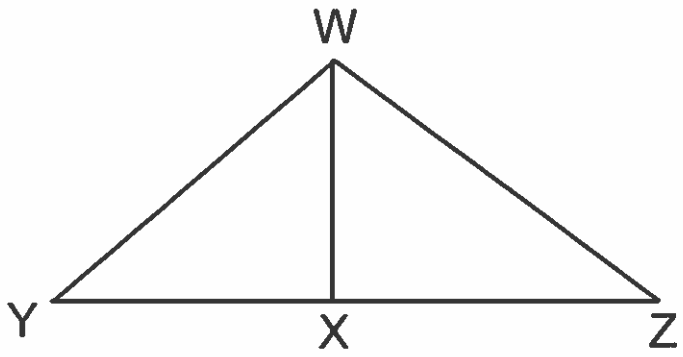


Given: $\overline{AB} \cong \overline{CB}$;

D is the midpoint of $\overline{AC}$

Prove: $\Delta ABD \cong \Delta CBD$

#5

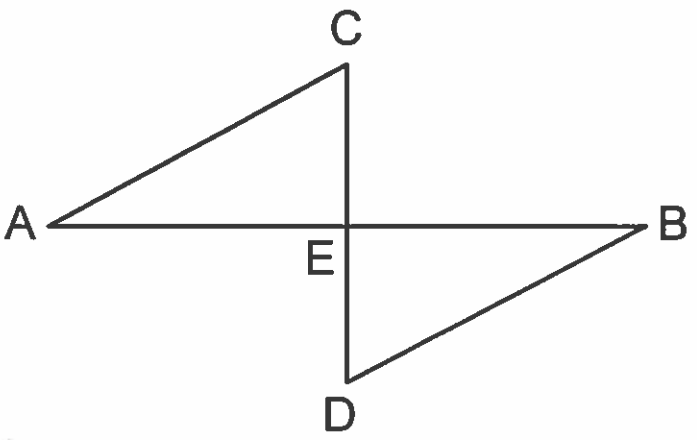


Given: $\overline{WX} \perp \overline{YZ}$;

$\overline{WY} \cong \overline{WZ}$

Prove: $\Delta WXY \cong \Delta WXZ$

#6



Given: $\overline{AB}$ is the perpendicular bisector of $\overline{CD}$;

$\angle C \cong \angle D$

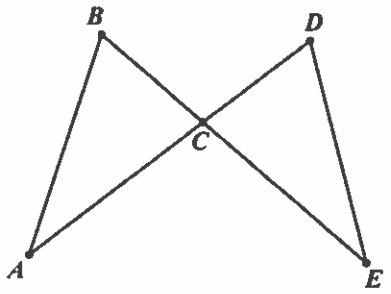
Prove: $\Delta ACE \cong \Delta BDE$

Geometry, Unit 5 – Congruent Triangles Proof Activity – Part I Name _____

For each problem, do the following:

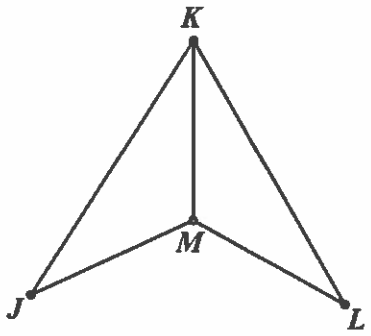
a. Show the given information in the diagram (using tick marks to show congruent sides and arcs to show congruent angles)
b. Show any other congruent parts you notice (from vertical angles, sides shared in common, or alternate interior angles with parallel lines)
c. Give the postulate or theorem that proves the triangles congruent (SSS, SAS, ASA, AAS, HL)
d. Finally, fill in the blanks to complete the proof.

1. Given: $\overline{BC} \cong \overline{DC}$; $\overline{AC} \cong \overline{EC}$
Prove: $\Delta BCA \cong \Delta DCE$



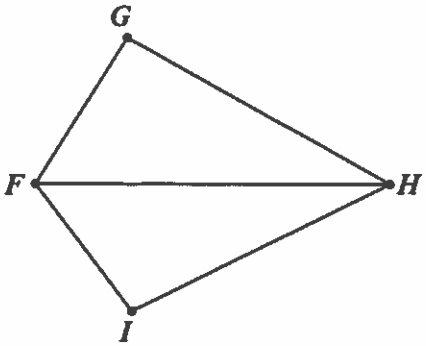
Statements	Reasons
1.	1. Given
2.	2. Vertical ∠s Theorem
3. $\Delta BCA \cong \Delta DCE$	3.

2. Given: $\overline{JK} \cong \overline{LK}$; $\overline{JM} \cong \overline{LM}$
Prove: $\Delta KJM \cong \Delta KLM$



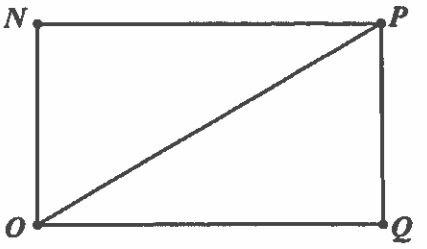
Statements	Reasons
1.	1.
2.	2. Reflexive Prop.
3.	3.

3. Given: $\angle G \cong \angle I$; $\overline{FH}$ bisects ∠GFI
Prove: $\Delta GFH \cong \Delta IFH$



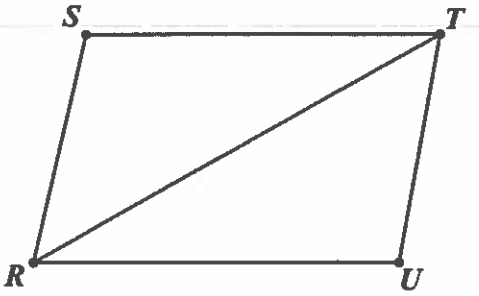
Statements	Reasons
1. $\angle G \cong \angle I$; $\overline{FH}$ bisects ∠GFI	1.
2. $\angle GFH \cong \angle IFH$	2. Def. of _____
3.	3. Reflexive Prop.
4.	4.

4. Given: $\angle N$ and $\angle Q$ are right angles; $\overline{NO} \cong \overline{PQ}$
Prove: $\Delta ONP \cong \Delta PQO$



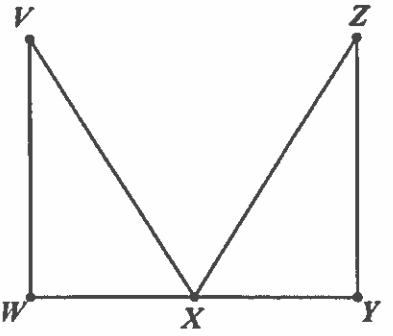
Statements	Reasons
1. $\angle N$ and $\angle Q$ are right angles	1.
2. ΔONP and ΔPQO are _____ triangles	2. Def. of right triangle
3.	3. Reflexive Prop.
4. $\overline{NO} \cong \overline{PQ}$	4.
5.	5.

5. Given: $\overline{ST} \parallel \overline{RU}$; $\overline{SR} \parallel \overline{TU}$
Prove: $\Delta SRT \cong \Delta UTR$



Statements	Reasons
1. $\overline{ST} \parallel \overline{RU}$	1.
2.	2. If lines $\parallel$, alt. int. $\angle s \cong$
3. $\overline{SR} \parallel \overline{TU}$	3.
4. $\angle SRT \cong \angle UTR$	4.
5.	5.
6.	6.

6. Given: $\angle W$ and $\angle Y$ are right angles; $\overline{VX} \cong \overline{ZX}$; X is the midpoint of $\overline{WY}$
Prove: $\Delta VWX \cong \Delta ZYX$



Statements	Reasons
1. $\angle W$ and $\angle Y$ are right angles	1.
2.	2. Def. of right triangle
3. $\overline{VX} \cong \overline{ZX}$; X is the midpoint of $\overline{WY}$	3.
4.	4. Def. of midpoint
5.	5.

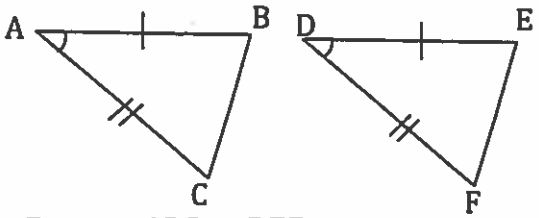
Proofs Involving Congruent Triangles

First, let's analyze some proofs.

This is easy! All you have to do is explain in plain English what is going on in the proofs. We'll look at some examples first.

AE. 1.

Given: $\overline{AB}\cong\overline{DE}$, $\overline{AC}\cong\overline{DF}$, and $\angle A\cong\angle D$



Prove: $\triangle ABC\cong\triangle DEF$

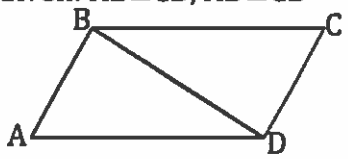
Statements	Reasons
1. $\overline{AB}\cong\overline{DE}$	1. Given
2. $\overline{AC}\cong\overline{DF}$	2. Given
3. $\angle A\cong\angle D$	3. Given
4. $\triangle ABC\cong\triangle DEF$	4. SAS

Analysis:

Working backward we must ask the key question, "How can we show that two triangles are congruent?" The answer? A triangle congruence theorem like SSS, SAS, ASA, AAS or HL. This gives us B1: $\triangle ABC\cong\triangle DEF$, by some property, but which one? To find out, start working forward. Listing all of the given information gives us a pair of angles $\angle A$ and $\angle D$ sandwiched between a pair of congruent sides $\overline{AB}\cong\overline{DE}$ and $\overline{AC}\cong\overline{DF}$. So this means we have $\triangle ABC\cong\triangle DEF$ by the SAS theorem which is B2: and the proof is complete.

AE. 2.

Given: $\overline{AB}\cong\overline{CD}$, $\overline{AD}\cong\overline{CB}$



Prove: $\triangle ABD\cong\triangle BCD$

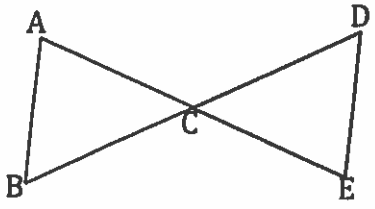
Statements	Reasons
1. $\overline{AB}\cong\overline{CD}$	1. Given
2. $\overline{AD}\cong\overline{CB}$	2. Given
3. $\overline{BD}\cong\overline{BD}$	3. Reflexive property
4. $\triangle ABD\cong\triangle CDB$	4. SSS

Analysis:

Working backward, we must ask the key question "How can we show that two triangles are congruent?" The answer? A triangle congruence theorem like SSS, SAS, ASA, AAS or HL. This gives us B1: $\triangle ABC\cong\triangle BCD$ bys ome property, but which one? Then start working forward. Listing all of the given information gives us two pairs of sides $\overline{AB}\cong\overline{CD}$ and $\overline{AD}\cong\overline{CB}$, but this is not enough. We need another pair of sides or an angle between them. Looking now at the diagram we have $\overline{BD}\cong\overline{BD}$ as a shared line. So this brings us to say $\triangle ABC\cong\triangle BCD$ by SSS which is B1 and the proof is complete.

AE. 3.

Given: $\overline{AE}$ Bisects $\overline{BD}$, $\angle B\cong\angle D$



Prove: $\triangle ABC\cong\triangle DBC$

Statements	Reasons
1. $\angle B\cong\angle D$	1. Given
2. $\overline{AC}$ Bisects $\overline{BD}$	2. Given
3. $\overline{BC}\cong\overline{DC}$	3. Definition of Bisect
4. $\angle ACB\cong\angle DCE$	4. Vertical angles
5. $\triangle ABC\cong\triangle DBC$	5. ASA

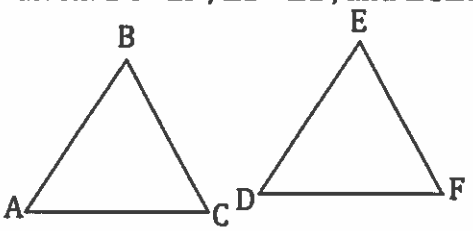
Analysis:

Working backward we must ask the key question, "How can we show that two triangles are congruent?" The answer? A triangle congruence theorem like SSS, SAS, ASA, AAS or HL. This gives us B1: $\triangle ABC\cong\triangle BCD$ by some property, but which one? Then start working forward. Listing all of the given information gives us a pair of angles $\angle B$ and $\angle D$, and $\overline{BD}$ and $\overline{AE}$ bisects $\overline{BD}$. If AE bisects $\overline{BD}$ then $\overline{BD}$ is cut in half at C so $\overline{BC}\cong\overline{DC}$! This is not enough though. Looking at the diagram we see vertical angles $\angle ACB\cong\angle DCE$, which gives us $\triangle ABC\cong\triangle BCD$ by the property ASA . This is B1 and the proof is complete.

Your turn! Write an analysis of each proof involving congruent triangles.

1. Analysis:

Given: $\overline{BC} \cong \overline{EF}$, $\angle B \cong \angle E$, and $\angle C \cong \angle F$

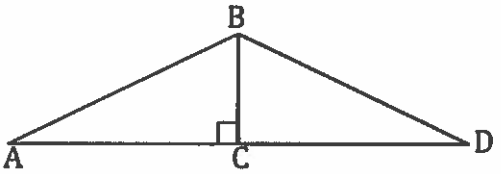


Prove: $\triangle ABC \cong \triangle DEF$

Statements	Reasons
1. $\overline{BC} \cong \overline{EF}$	1. Given
2. $\angle B \cong \angle E$	2. Given
3. $\angle C \cong \angle F$	3. Given
4. $\triangle ABC \cong \triangle DEF$	4. ASA

2. Analysis:

Given: $\overline{AB} \cong \overline{BD}$

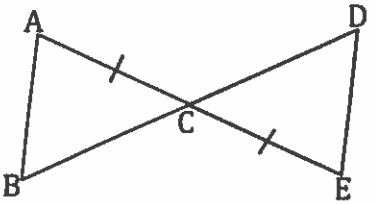


Prove: $\triangle ABD \cong \triangle BCD$

Statements	Reasons
1. $\overline{AB} \cong \overline{BD}$	1. Given
2. $\overline{BC} \cong \overline{BC}$	2. Reflexive property
3. $\triangle ABC \cong \triangle DBC$	3. HL

3. Analysis:

Given $\overline{AB} \parallel \overline{ED}$, $\overline{AC} \cong \overline{EC}$



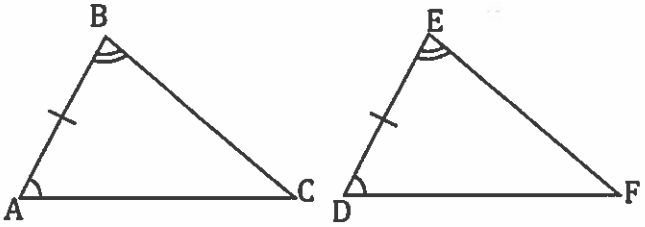
Prove: $\triangle ABC \cong \triangle EDC$

Statements	Reasons
1. $\overline{AB} \parallel \overline{ED}$	1. Given
2. $\overline{AC} \cong \overline{EC}$	2. Given
3. $\angle A \cong \angle E$	3. Alternate Interior angles
4. $\angle ACB \cong \angle DCE$	4. Vertical angles
5. $\triangle ABC \cong \triangle DBC$	5. ASA

For these fill in any missing statements or reasons.

1.

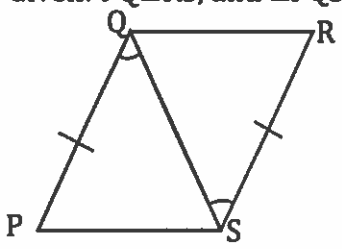
Given: $\overline{AB}\cong\overline{DE}$, $\angle B\cong\angle E$, and $\angle A\cong\angle D$



Prove: $\triangle ABC\cong\triangle DBC$

Statements	Reasons
1. $\overline{AB}\cong\overline{DE}$	1. Given
2.	2.Given
3. $\angle A\cong\angle D$	3.
4. $\triangle ABC\cong\triangle DEF$	4.

2. Given: $\overline{PQ}\cong\overline{RS}$, and $\angle PQS\cong\angle RSQ$

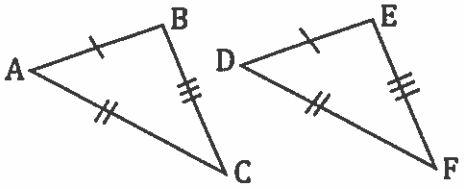


Prove: $\triangle ABC\cong\triangle DBC$

Statements	Reasons
1.	1. Given
2.	2. Given
3. $\overline{QS}\cong\overline{QS}$	3.
4. $\triangle PQS\cong\triangle RSQ$	4.

3.

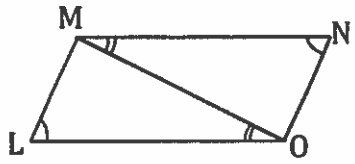
Given: $\overline{AB}\cong\overline{DE}$, $\overline{AC}\cong\overline{DF}$, and $\overline{BC}\cong\overline{EF}$



Prove: $\triangle ABD\cong\triangle DEF$

Statements	Reasons
1. $\overline{AB}\cong\overline{DE}$	1.
2.	2.
3.	3.
4.	4. SSS

4. Given: $\angle L\cong\angle N$, $\angle LOM\cong\angle NMO$

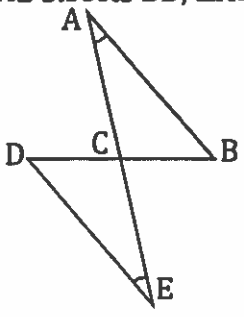


Prove: $\triangle LMO\cong\triangle NOM$

Statements	Reasons
1.	1.
2.	2. Given
3.	3. Reflexive Property
4. $\triangle LMO\cong\triangle NOM$	4.

5.

Given: $\overline{AE}$ bisects $\overline{BD}$, $\angle A\cong\angle E$

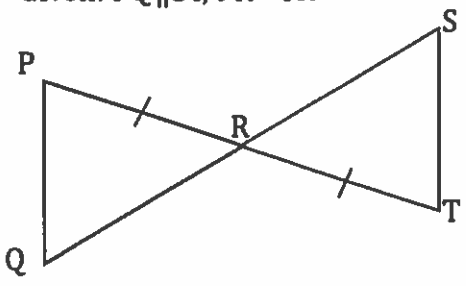


Prove: $\triangle ABC\cong\triangle EDC$

Statements	Reasons
1. $\angle A\cong\angle E$	1.
2.	2. Given
3.	3. Definition of Bisect
4. $\angle ACB\cong\angle DCE$	4.
5. $\triangle ABC\cong\triangle EDC$	5.

6.

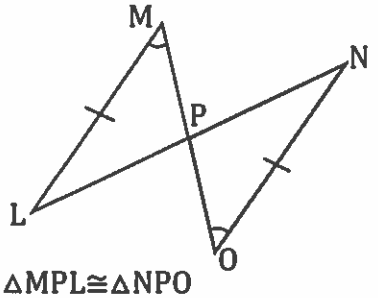
Given: $\overline{PQ}\parallel\overline{ST}$, $\overline{PR}\cong\overline{TR}$



Prove: $\triangle PQR\cong\triangle TSR$

Statements	Reasons
1. $\overline{PR}\cong\overline{TR}$	1.
2.	2. Given
3. $\angle P\cong\angle T$	3.
4. $\angle ACB\cong\angle DCE$	4.
5.	5. ASA

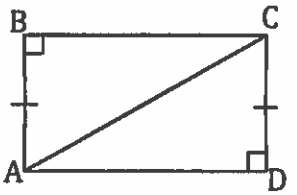
7. Given: $\overline{LM} \cong \overline{NO}$, and $\angle M \cong \angle O$



Prove: $\triangle MPL \cong \triangle NPO$

Statements	Reasons
1. $\overline{LM} \cong \overline{NO}$	1.
2.	2. Given
3.	3.
4.	4. AAS

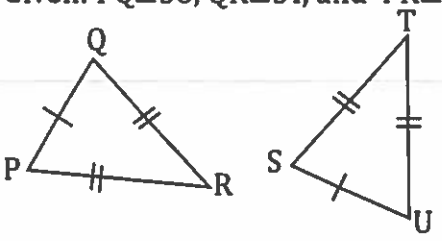
8. Given: $\overline{AB} \cong \overline{DC}$



Prove: $\triangle ABC \cong \triangle CDA$

Statements	Reasons
1.	1. Given
2. $\overline{AC} \cong \overline{AC}$	2.
3. $\triangle ABC \cong \triangle CDA$	3.

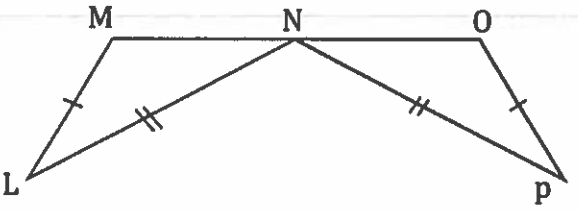
9. Given: $\overline{PQ} \cong \overline{SU}$, $\overline{QR} \cong \overline{ST}$, and $\overline{PR} \cong \overline{TU}$



Prove: $\triangle PQR \cong \triangle UST$

Statements	Reasons
1.	1. Given
2.	2. Given
3.	3.
4. $\triangle PQR \cong \triangle UST$	4.

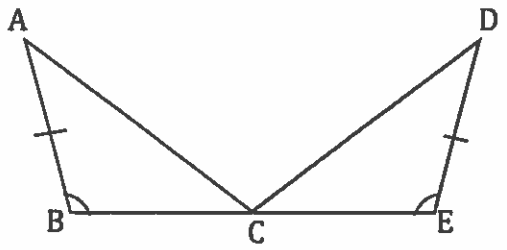
10. Given: N is the midpoint of $\overline{MO}$, $\overline{LM} \cong \overline{OP}$, and $\overline{LN} \cong \overline{PN}$



Prove: $\triangle LMN \cong \triangle PON$

Statements	Reasons
1. $\overline{LM} \cong \overline{OP}$	1. Given
2. $\overline{LN} \cong \overline{PN}$	2.
3. N is the Midpoint of $\overline{MO}$	3. Given
4.	4. Midpoint
5.	5. SSS

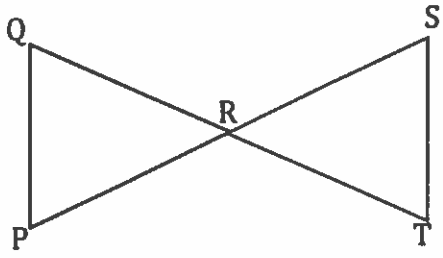
11. Given: C is the midpoint of $\overline{BE}$, $\angle B \cong \angle E$, and $\overline{AB} \cong \overline{DE}$



Prove: $\triangle ABC \cong \triangle DEC$

Statements	Reasons
1. $\angle B \cong \angle E$	1.
2. $\overline{AB} \cong \overline{DE}$	2.
3.	3. Given
4.	4. Midpoint
5. $\triangle ABC \cong \triangle DEC$	5. SAS

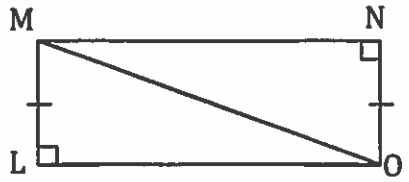
12. Given: $\overline{QT}$ bisects $\overline{SP}$, $\overline{SP}$ bisects $\overline{QT}$



Prove: $\triangle QRP \cong \triangle SRT$

Statements	Reasons
1. $\overline{QT}$ bisects $\overline{SP}$	1. Given
2.	2. Given
3. $\overline{QR} \cong \overline{TR}$	3. Definition of Bisect
4. $\overline{PR} \cong \overline{SR}$	4.
5.	5. Vertical Angles
6. $\triangle QRP \cong \triangle SRT$	6.

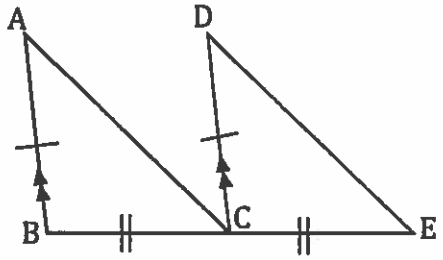
13. Given: $\overline{LM} \cong \overline{NO}$



Prove: $\triangle LMO \cong \triangle NOM$

Statements	Reasons
1. $\overline{LM} \cong \overline{NO}$	1.
2.	2.
3.	3.

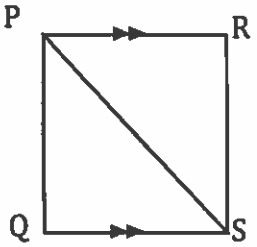
14. Given: $\overline{AB} \cong \overline{DC}$, $\overline{AB} \parallel \overline{DC}$, and $\overline{BC} \cong \overline{CE}$



Prove: $\triangle ABC \cong \triangle DCE$

Statements	Reasons
1. $\overline{AB} \cong \overline{DC}$	1. Given
2.	2. Given
3.	3. Given
4.	4. Corresponding Angles
5. $\triangle ABC \cong \triangle DCE$	5.

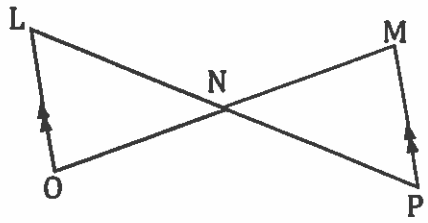
15. Given: $\overline{PR} \parallel \overline{QS}$, $\angle QPS \cong \angle RSP$



Prove: $\triangle PQS \cong \triangle SRP$

Statements	Reasons
1. $\overline{PR} \parallel \overline{QS}$	1.
2. $\angle QPS \cong \angle RSP$	2.
3. $\angle PSQ \cong \angle SPR$	3. Alternate Interior
4.	4. Reflexive Property
5. $\triangle ABD \cong \triangle CDB$	5.

16. Given: $\overline{LP}$ bisects $\overline{MO}$, $\overline{LO} \parallel \overline{MP}$

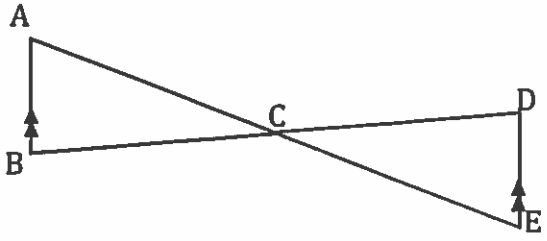


Prove: $\triangle LNO \cong \triangle MNP$

Statements	Reasons
1.	1. Given
2.	2. Given
3. $\overline{LN} \cong \overline{PN}$	3.
4.	4. Alternate Interior
5.	5. Vertical Angles
6.	6. ASA

17.

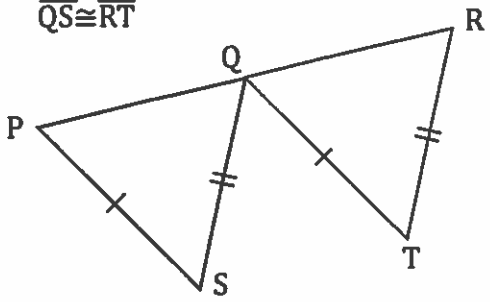
Given: $\overline{AE}$ bisects $\overline{BD}$, $\overline{AB} \parallel \overline{DE}$



Prove: $\triangle ABC \cong \triangle DCE$

Statements	Reasons
1. $\overline{AE}$ bisects $\overline{BD}$	1.
2.	2. Given
3. $\overline{BC} \cong \overline{DC}$	3.
4. $\angle ACB \cong \angle DCB$	4.
5.	5. Alternate Interior
6.	6. ASA

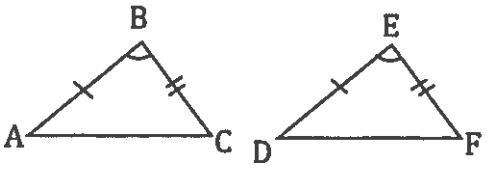
18. Given: Q is the midpoint of $\overline{PR}$. $\overline{PS} \cong \overline{QT}$ and $\overline{QS} \cong \overline{RT}$



Prove: $\triangle PQS \cong \triangle RQT$

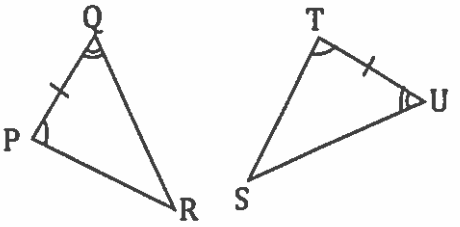
Statements	Reasons
1.	1. Given
2.	2. Given
3. $\overline{QS} \cong \overline{RT}$	3.
4.	4. Midpoint
5. $\triangle ABC \cong \triangle DBC$	5.

19. Given: $\overline{AB} \cong \overline{DE}$, $\overline{BC} \cong \overline{EF}$, and $\angle B \cong \angle E$



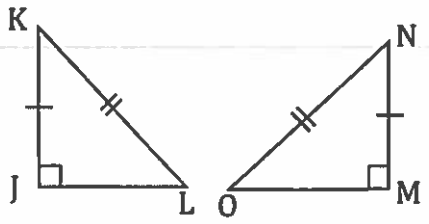
Prove: $\triangle ABC \cong \triangle DEF$

20. Given: $\overline{PQ} \cong \overline{TU}$, $\angle P \cong \angle T$, and $\angle Q \cong \angle U$



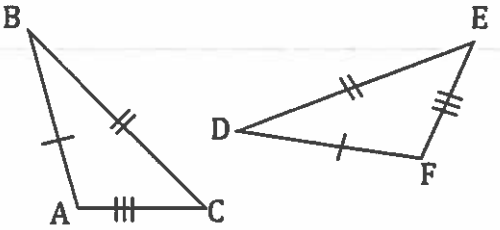
Prove: $\triangle PQR \cong \triangle TUS$

21. Given: $JK \cong MN$, $KL \cong NO$



Prove: $\triangle JKL \cong \triangle MNO$

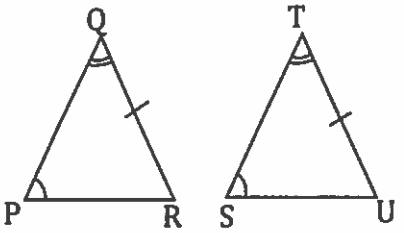
22. Given: $\overline{AB} \cong \overline{DF}$, $\overline{BC} \cong \overline{DE}$, and $\overline{AC} \cong \overline{EF}$



Prove: $\triangle ABD \cong \triangle FDE$

23.

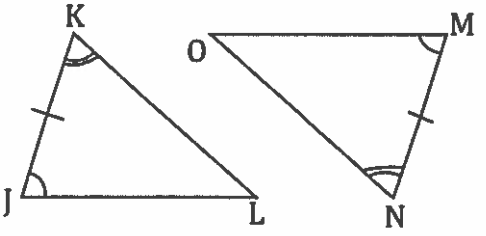
Given: $\angle P \cong \angle S$, $\angle Q \cong \angle T$, and $\overline{QR} \cong \overline{TU}$



Prove: $\triangle PQR \cong \triangle STU$

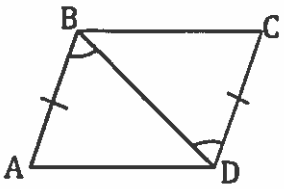
24.

Given: $\angle J \cong \angle M$, $\overline{JK} \cong \overline{MN}$ and $\angle K \cong \angle N$



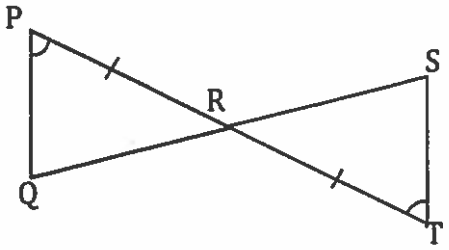
Prove: $\triangle JKL \cong \triangle MNO$

25. Given: $\overline{AB} \cong \overline{CD}$, $\angle ABD \cong \angle CDB$



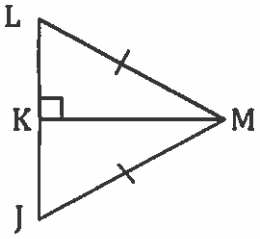
Prove: $\triangle ABD \cong \triangle CDB$

26. Given: $\overline{PR} \cong \overline{TR}$, $\angle P \cong \angle T$



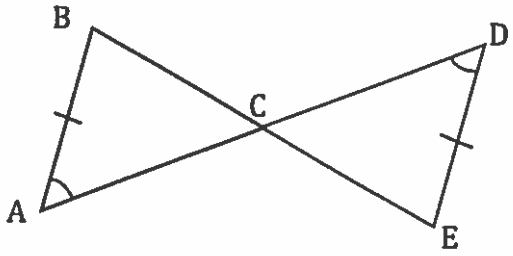
Prove: $\triangle ABC \cong \triangle DBC$

27. Given: $\overline{LM} \cong \overline{JM}$



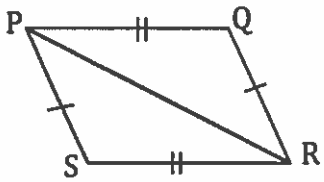
Prove: $\triangle LKM \cong \triangle JKM$

28. Given: $\overline{AB} \cong \overline{ED}$, $\angle A \cong \angle D$



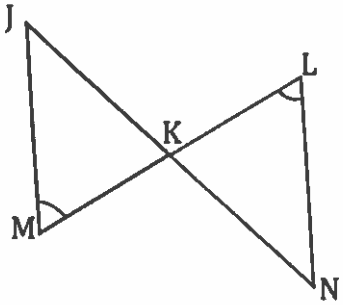
Prove: $\triangle ABC \cong \triangle DCE$

29. Given: $\overline{PS} \cong \overline{QR}$, $\overline{PQ} \cong \overline{SR}$



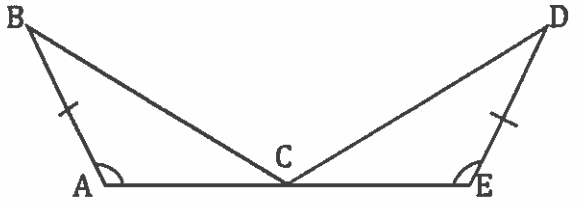
Prove: $\triangle PRS \cong \triangle RPQ$

30. Given: $\overline{JN}$ Bisects $\overline{ML}$, $\angle M \cong \angle L$



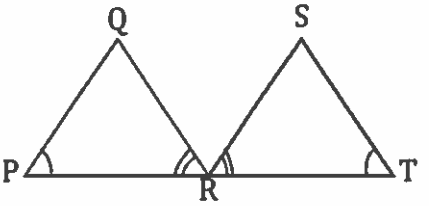
Prove: $\triangle MJK \cong \triangle LNK$

31. Given: C is the midpoint of $\overline{AE}$, $\overline{BA} \cong \overline{DE}$, and $\angle A \cong \angle E$



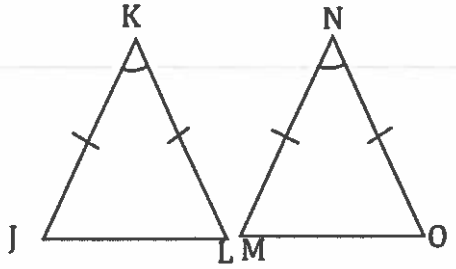
Prove: $\triangle ABC \cong \triangle EDC$

32. Given: R is the midpoint of $\overline{PT}$, $\angle P \cong \angle T$, and $\angle PRQ \cong \angle TRS$



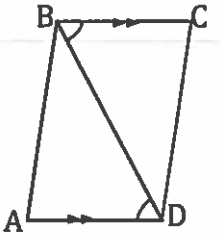
Prove: $\triangle PQR \cong \triangle TSR$

33. Given: $\angle K \cong \angle N$, $\overline{JK} \cong \overline{MN}$, $\overline{KL} \cong \overline{NO}$



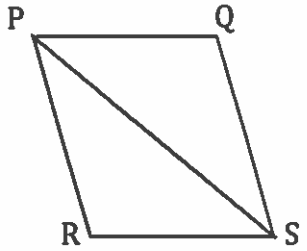
Prove: $\triangle JKL \cong \triangle MNO$

34. Given: $\overline{BA} \| \overline{CD}$ $\angle ADB \cong \angle CBD$



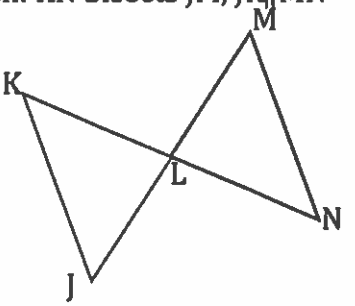
Prove: $\triangle ABD \cong \triangle CDB$

35. Given: PQRS is a parallelogram



Prove: $\triangle RPS \cong \triangle QSP$

36. Given: $\overline{KN}$ bisects $\overline{JM}$, $\overline{JK} \| \overline{MN}$



Prove: $\triangle JKL \cong \triangle MNL$